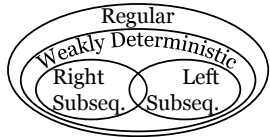


Introduction

- Input-output mappings can be classified hierarchically by computational complexity (Chomsky 1956)



- All attested phonological mappings are a proper subset of the class of regular input-output mappings (Heinz 2011)
- (Un)attestedness of certain phonological patterns can be

attributed to computational complexity of input-output mappings (Heinz & Lai 2013, Jardine 2016)

- Sour-grapes-like spreading: spread phonological property throughout domain or not at all (Padgett 1995; Wilson 2003)

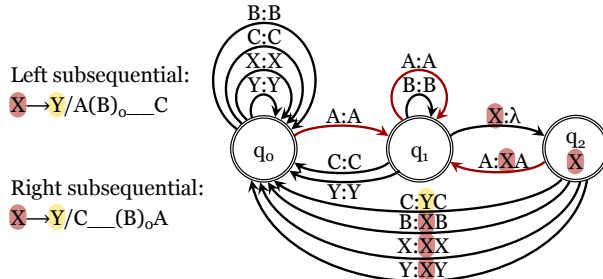
Proposals

Different sour-grapes-like patterns characterized by different degrees of computational complexity:

- False sour grapes** (attested) is relatively less complex due to zone of predictability local to potential triggers of spreading
- True sour grapes** (unattested) has no zone of predictability and is relatively more complex

Computational Complexity

- Input-output mapping of strings can be described by transformational rules or by finite state transducers
- Properties of rules/transducers indicate computational complexity of input-output mappings
- All regular mappings can be decomposed into left and right subsequential mappings (those with unbounded amount of material on only one side of the target) (Elgot & Mezei 1965)



- Weakly deterministic mappings (Heinz & Lai 2013) can be decomposed into left- and right-subsequential functions that:
 - Do not change the number of symbols in a string
 - Are alphabet-preserving (do not introduce new symbols)

Copperbelt Bemba Tone Spreading

- Copperbelt Bemba (Bantu; Zambia) exhibits ternary and unbounded spreading of H tones (Bickmore & Kula 2013)
- Final H spreads unboundedly to following tone bearing units:

H H H H
/bá-ka-fik-a/ → [bá-ká-fik-á] 'they will hate'

- Non-final H spreads only to two additional tone bearing units:

H H H H L L L H
/bá-ka-londolol-a kó/ → [bá-ká-lóndòlòl-à kó]
'they will introduce them'

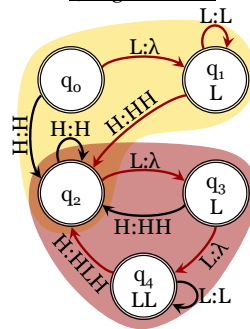
- Previous claim: sour-grapes-like unbounded tone spreading in Copperbelt Bemba is not weakly deterministic (Jardine 2016)
- Whether H triggers unbounded spreading is not known until rest of word is scanned for presence of following blocking H

Copperbelt Bemba tone spreading:

- Is a case of **false sour grapes** spreading
- Can be characterized as a weakly deterministic input-output mapping

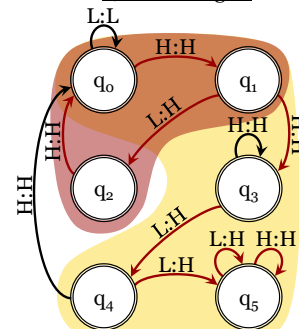
- Copperbelt Bemba: H spreading to two following tone bearing units provides predictable substring that can be used to mark up final H as successful trigger of unbounded tone spreading
- Zone of predictability:** predictable substring local to potential trigger of spreading that can be utilized for mark-up

1) Right to Left:



- Final H (successful trigger) marked up with predictable substring HLLL
- HLLL maps to HHHH, followed only by Hs

2) Left to Right:



- Non-final H (unsuccessful trigger) marked up with predictable substring HLH
- HLH maps to HHH

- False sour grapes:** zone of predictability local to potential trigger allows transducer to distinctly mark up triggers and non-triggers of unbounded tone spreading

True Sour Grapes Spreading

- True sour grapes:** no zone of predictability local to potential trigger results in mapping that is not weakly deterministic
- Potential undergoer U preceded at any distance by trigger T assimilates to the trigger

T U U U # → T T T T #

- If blocker B appears anywhere after a trigger T, no potential undergoers U assimilate to the trigger

T U U B # → T U U B #

- Successful mark-up strategy must distinguish unsuccessful triggers T_U (T followed by blocker) from successful triggers T_S (T not followed by blocker)

$T \rightarrow T_U / _ (U, T)_o B$ $T \rightarrow T_S / _ (U, T)_o \#$

- Using only symbols in alphabet, right to left transducer must mark up successful trigger and surrounding symbols (e.g., T and two following symbols) as some substring M (e.g., TUT)

$T(U, T)(U, T) \rightarrow M / _ (U, T)_o \#$

- Left to right transducer triggers spreading from M and all symbols in M surface as T

$U \rightarrow T / M(U, T)_o _ _$ $M \rightarrow T T T$

- But without **zone of predictability** local to potential trigger, there is no mark-up substring M that we can use while maintaining contrastiveness of underlying M before blockers

$MU(U)_o B \rightarrow TTT(T)_o B$
 $NU(U)_o B \rightarrow MU(U)_o B$
 $NU(U)_o B \rightarrow NU(U)_o B$

True sour grapes spreading cannot be rendered weakly deterministic using a zone of predictability

Conclusion & Future Work

- Main claim: sour-grapes-like patterns of spreading are only attested if they involve **zones of predictability**, rendering their mappings weakly deterministic
- Copperbelt Bemba tone spreading represents a case of weakly deterministic **false sour grapes** spreading
- Possible additional cases of false sour grapes:
 - Tutrugbu ATR harmony (McCollum et al. 2018)
 - Tuyuca nasal harmony? (Barnes 1996)
- Open questions for future work:
 - Do learners (and learning algorithms) make use of zones of predictability?
 - How do zones of predictability affect computational complexity of other phonological processes?

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